Sequential & Temporally-Delayed Learning

- 1. The Problem.
- 2. Sequential Learning & Context.
- 3. Temporally-delayed Learning & Reinforcement.

generalize to new stimuli. Error-driven + Hebbian: Solve tasks, learn systematic representations,

What's left?...

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What's left?...

lime!

Currently: networks learn immediate consequence of a given input.

- What if current input only makes sense as part of a sequence of inputs (e.g., language, social interactions)?
- What if the consequence of this input comes later (e.g., school/work,

How do we do it?

For example:

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For example:

My favorite color is purple.

How do we do it?

For example:

My favorite color is purple. Purple my color favorite is.

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My favorite color is purple. Purple my color favorite is. Is my purple color favorite.

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My favorite color is purple.
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The girl picked up the pen.

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The girl picked up the pen.
The pig raced around the pen.

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We represent the *context*, not just the current input.

How do we do it?

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My favorite color is purple. Purple my color favorite is. Is my purple color favorite. Is purple my color favorite.

The girl picked up the pen.
The pig raced around the pen.

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in language, social interactions, driving (who goes at a 4-way stop?)

Representing Context for Sequence Learning

How does the brain do it?
How would we get our models to do it?

Representing Context for Sequence Learning

How does the brain do it?

How would we get our models to do it?

Add layers to keep track of context (prefrontal cortex; hippocampus...).

BTXSE BPVPSE BTSXXTVVE BPTVPSE

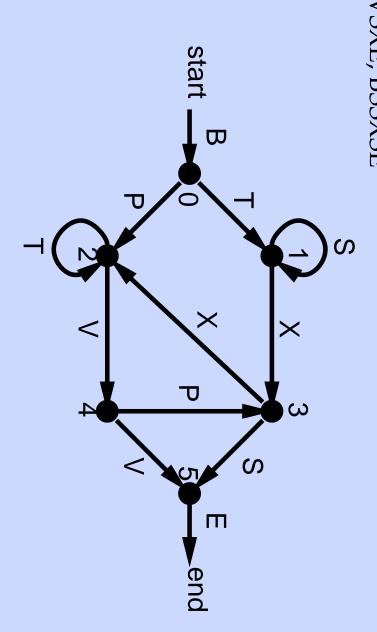
BTXSE
BPVPSE
BTSXXTVVE
BPTVPSE

TSXSE BTXXTTVVE Which of the following sequences are allowed?:

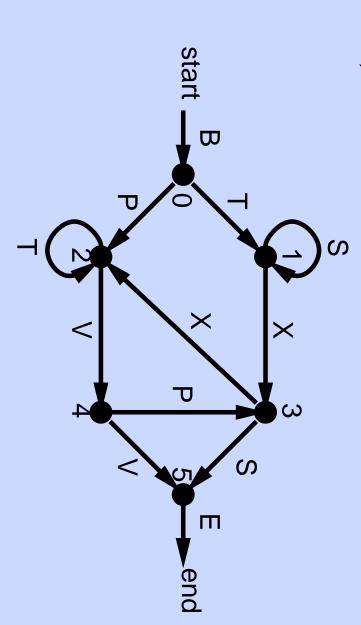
VVSXE BSSXSE

BTXSE, BPVPSE, BTSXXTVVE, BPTVPSE, BTXXTTVVE TSXSE, VVSXE, BSSXSE

BTXSE, BPVPSE, BTSXXTVVE, BPTVPSE, BTXXTTVVE TSXSE, VVSXE, BSSXSE



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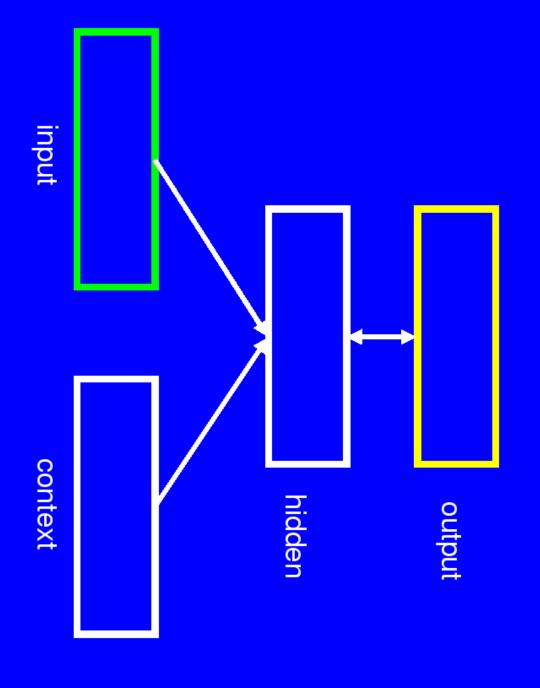
that follow grammar). We implicitly learn such grammars (e.g., pressing buttons faster to letters

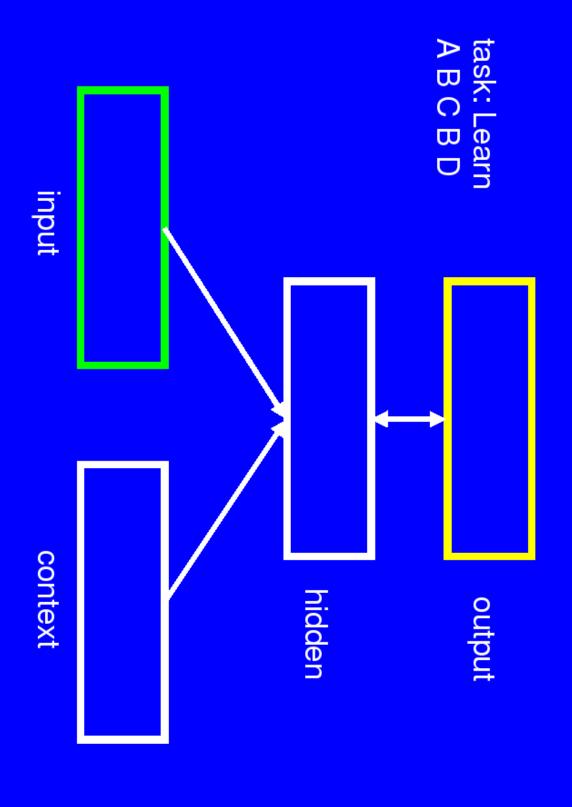
Time & Sequences

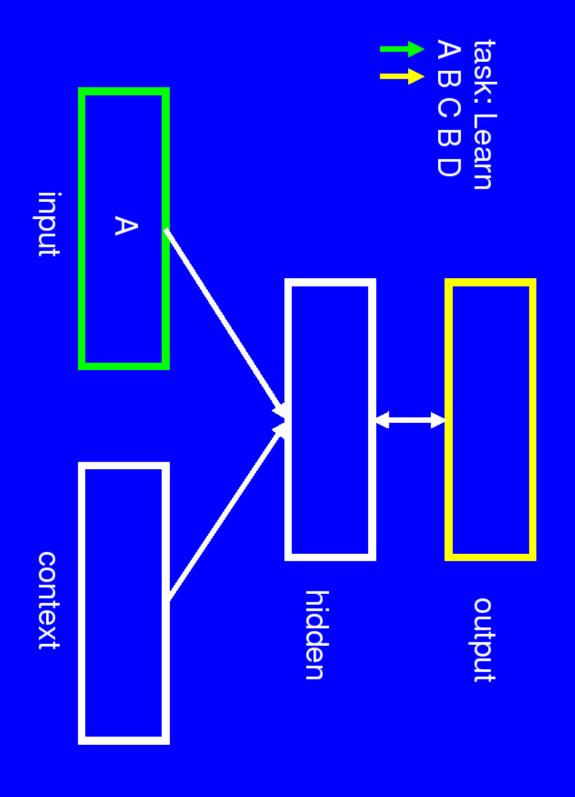
Currently: networks learn immediate consequence of a given input.

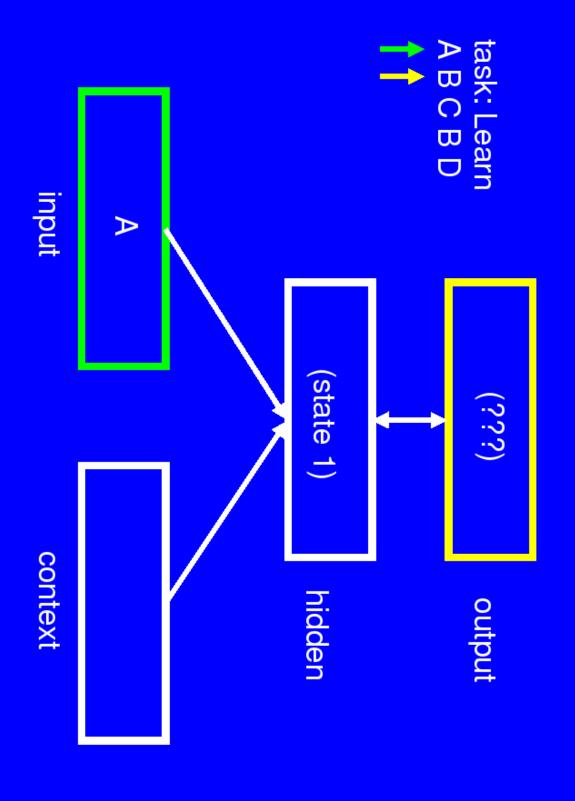
sequence of inputs? (context) What if current input only makes sense as part of a temporally-extended

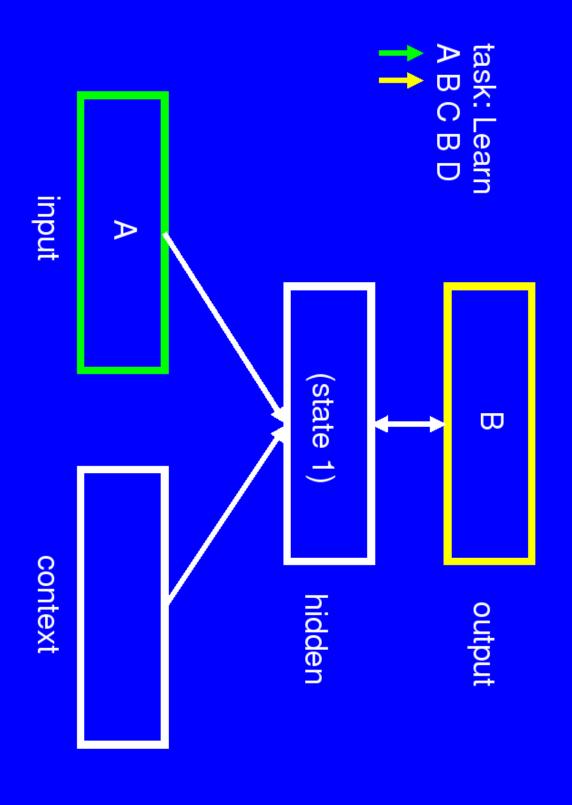
What if the consequence of this input comes later in time? (next week)

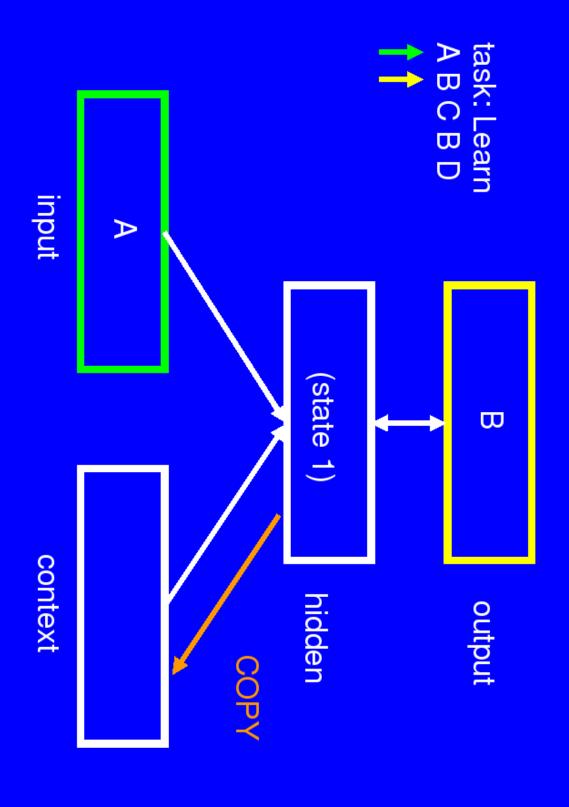


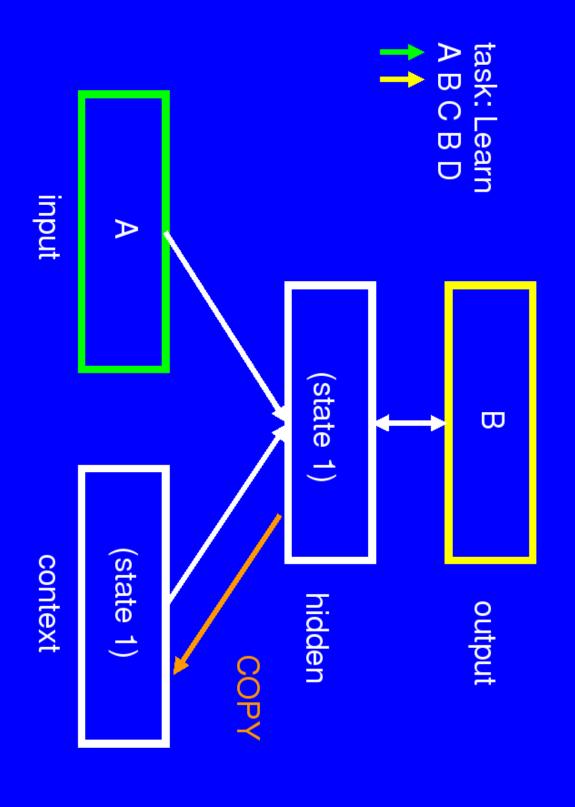


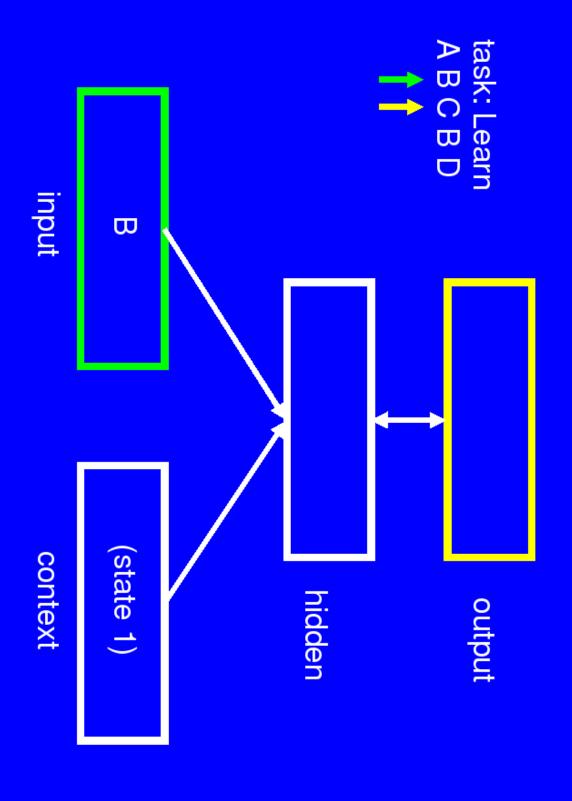


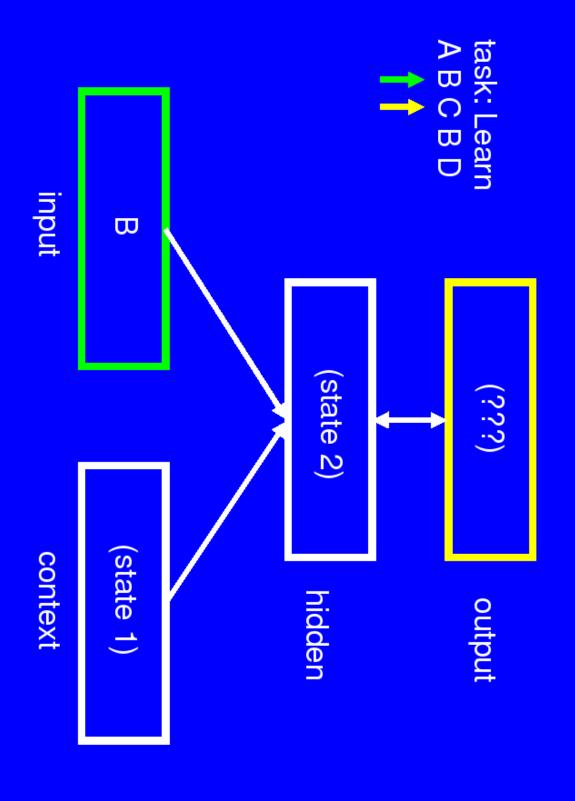


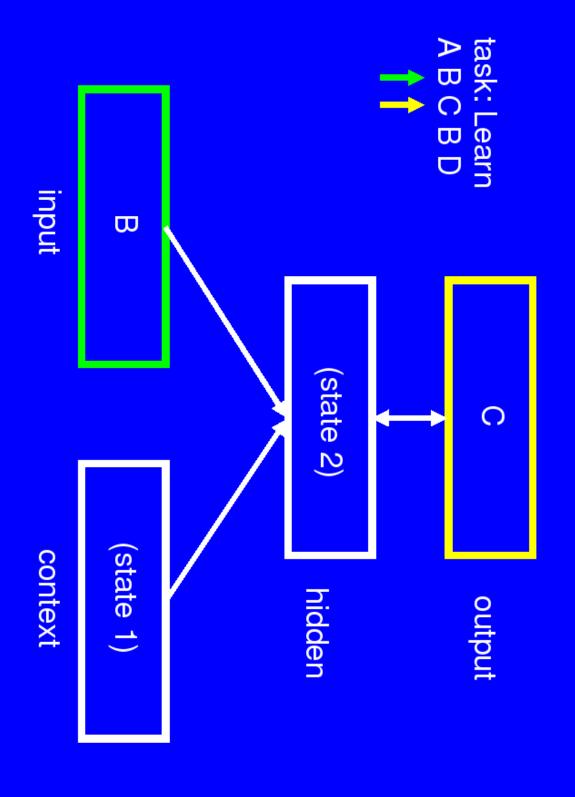


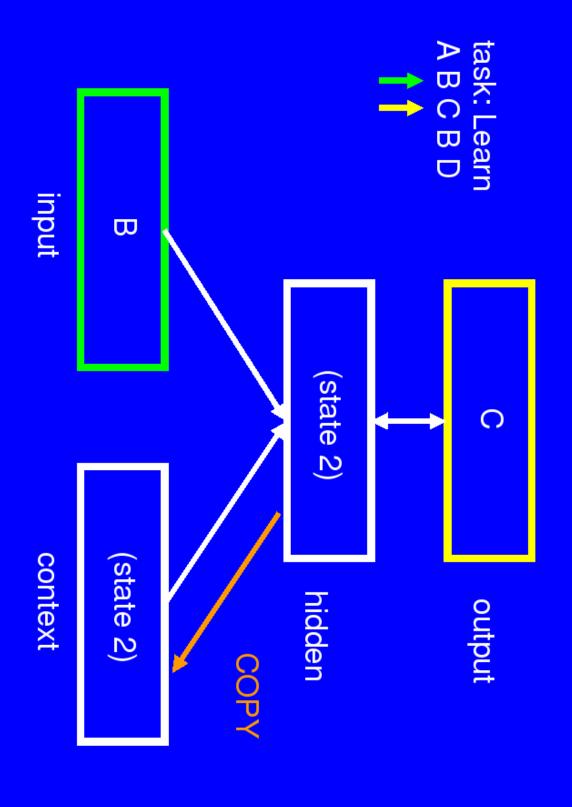


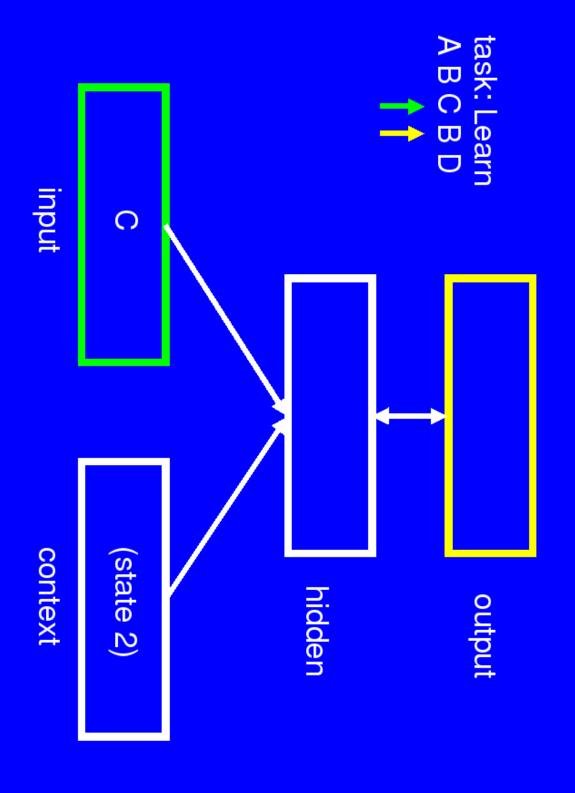


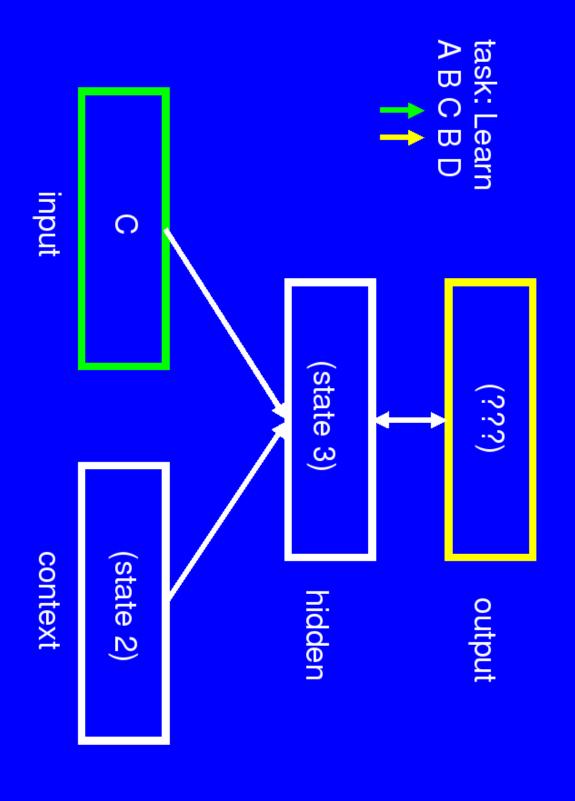


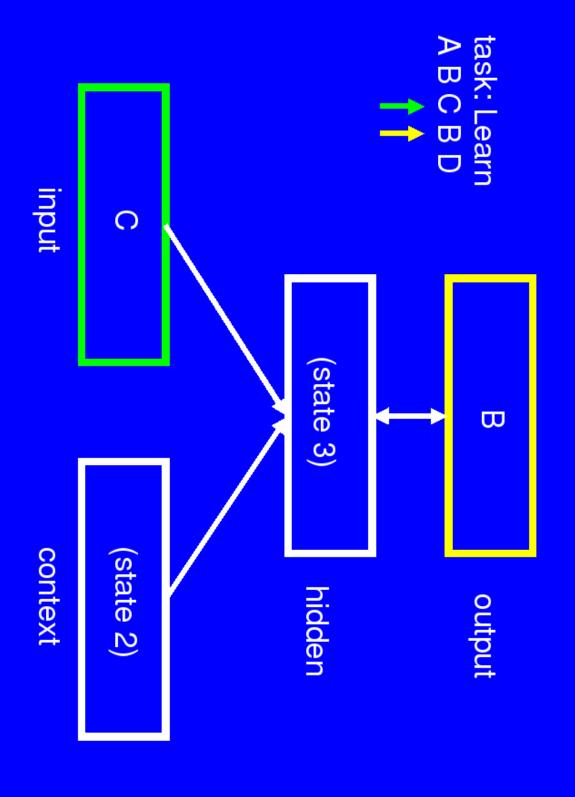


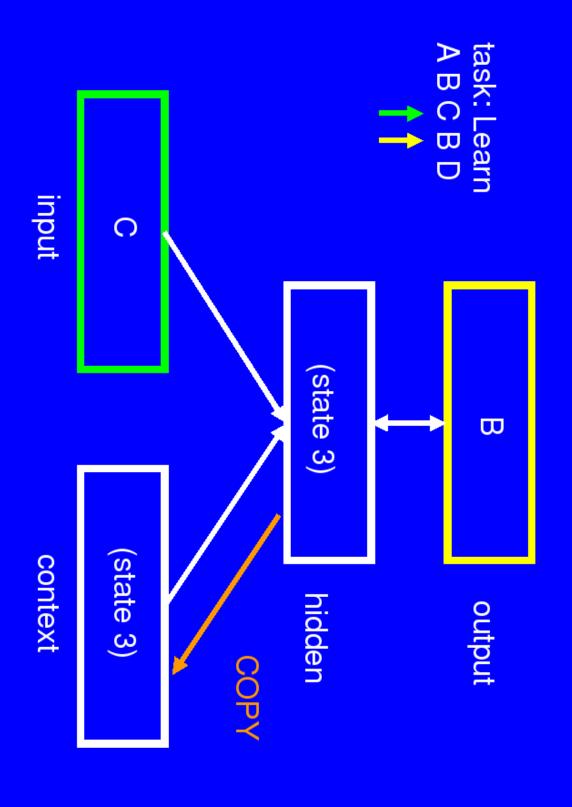


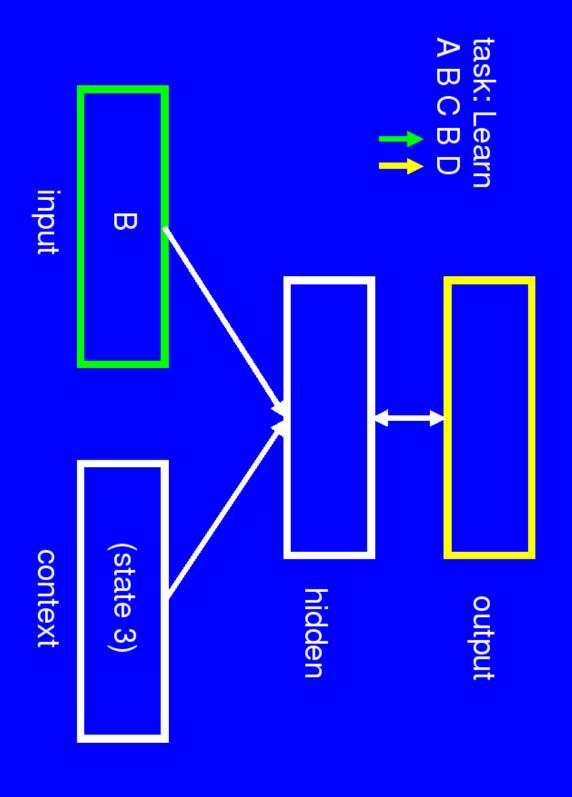


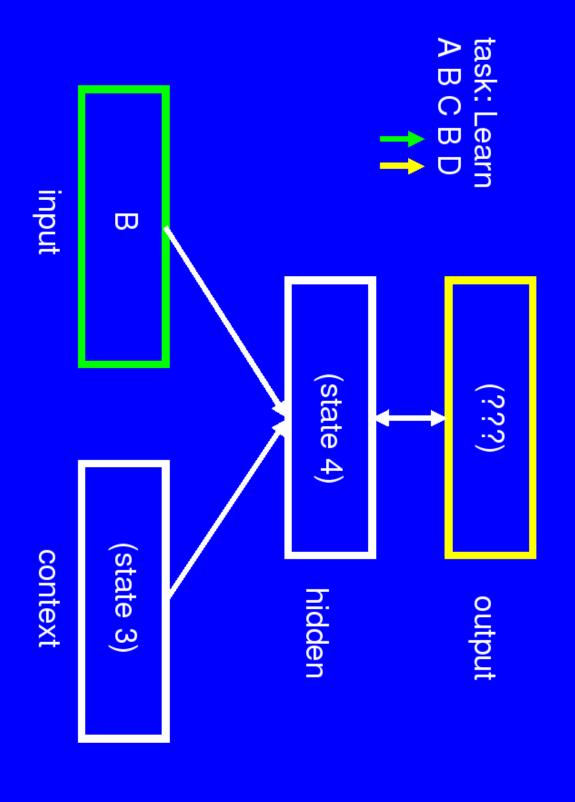


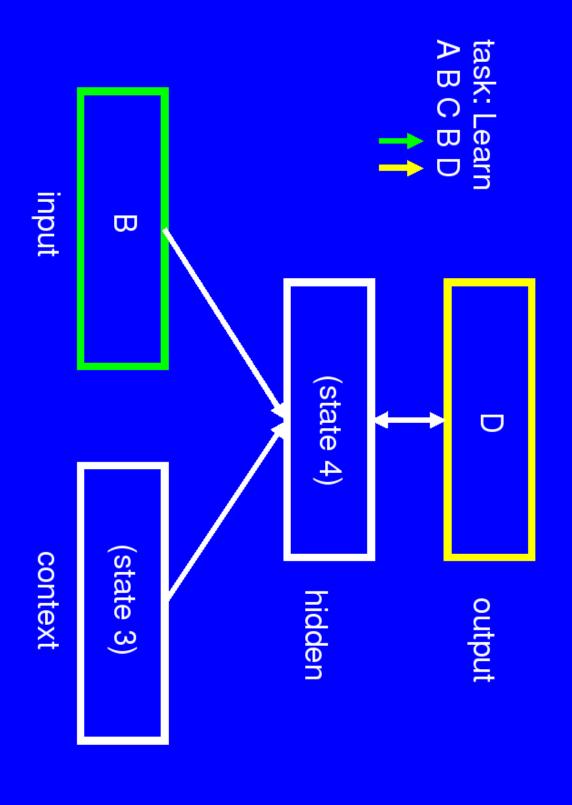






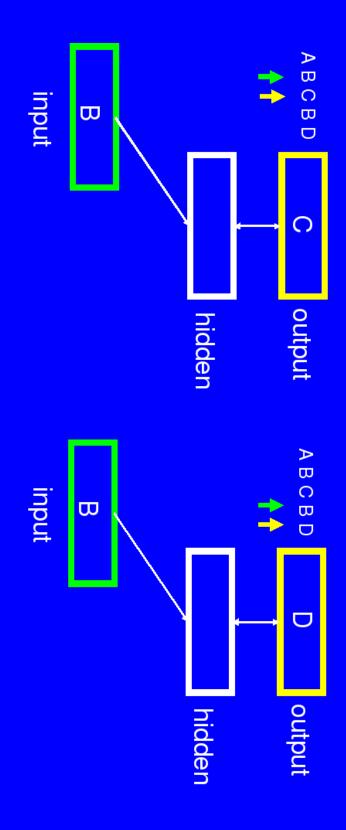






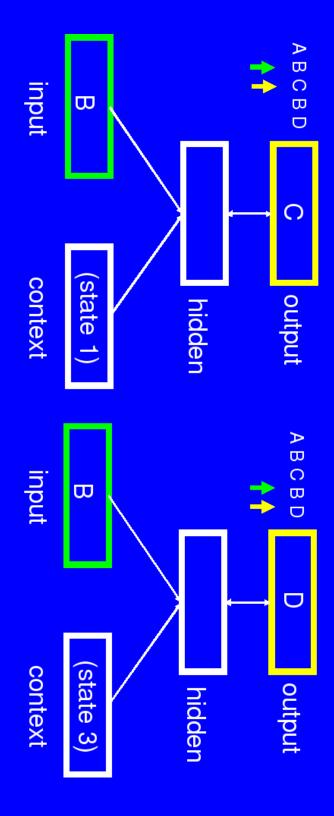
Simple Recurrent Network: Summary

- step. Carries forward information by means of a context layer that contains the hidden representation from the previous time
- This hidden representation serves to disambiguate the input

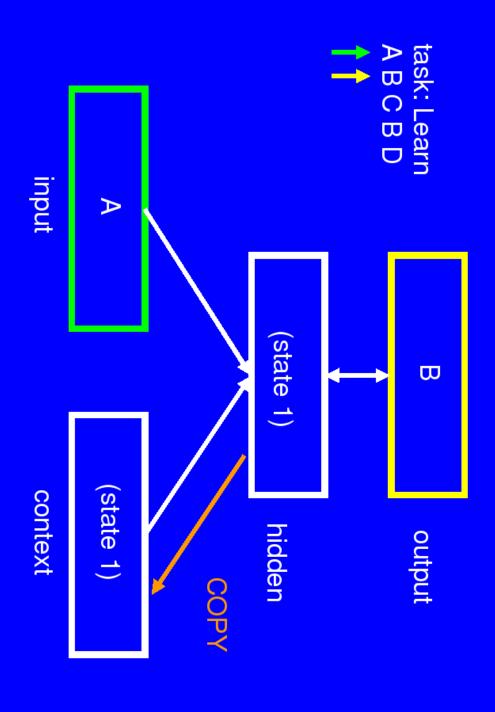


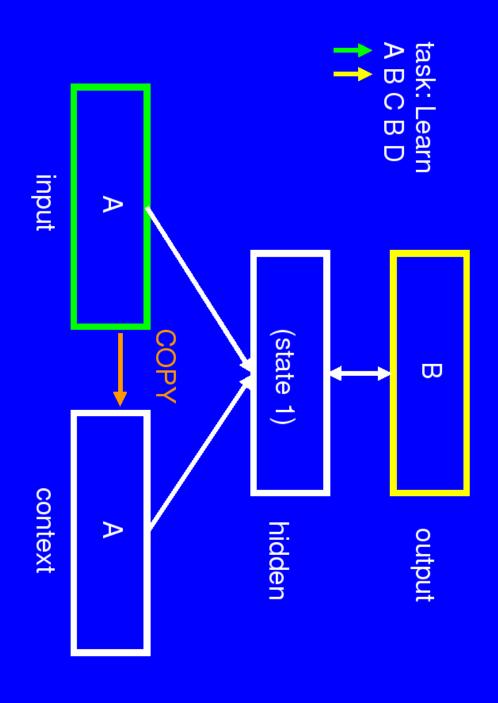
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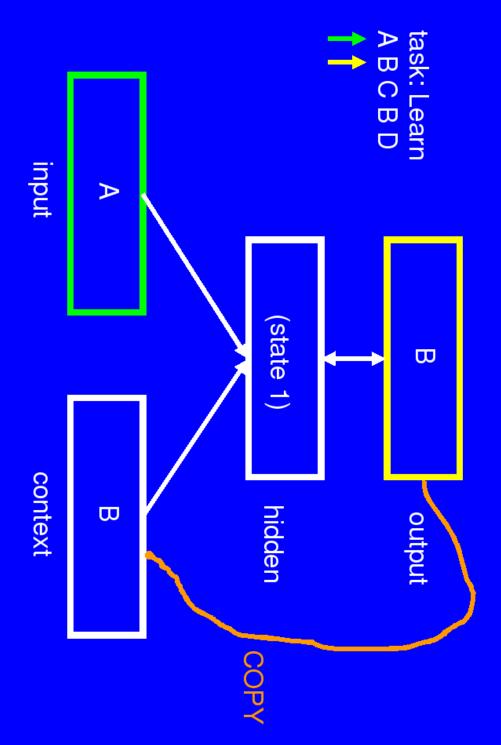
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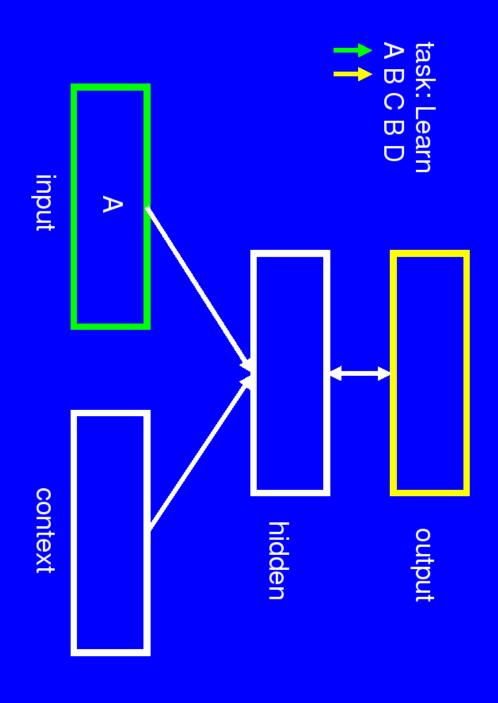


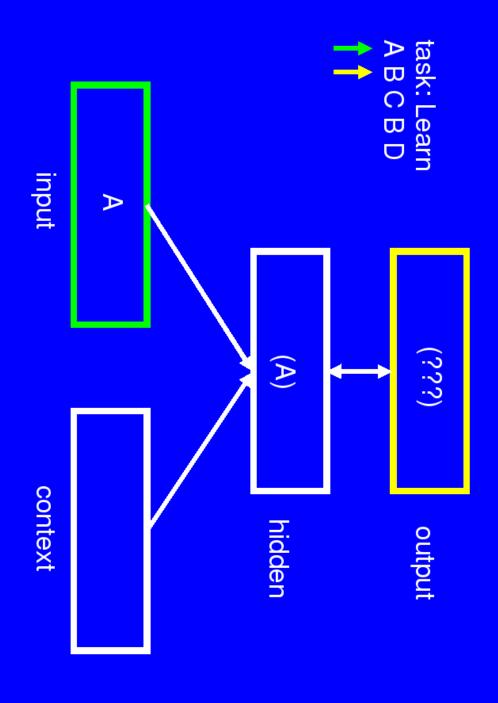
Why Copy the Hidden Representation?

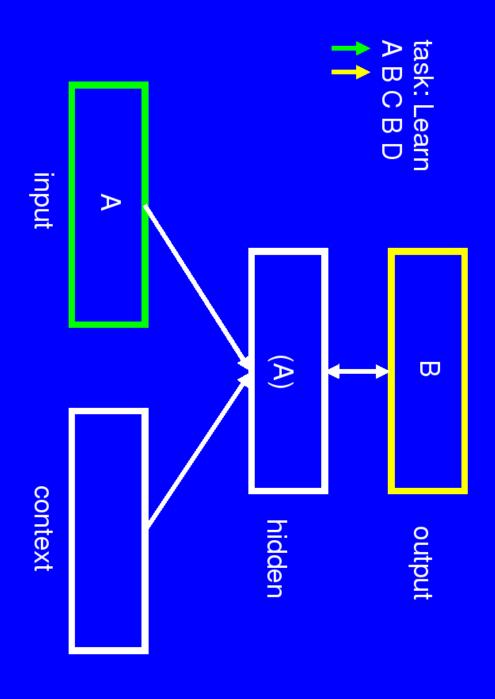


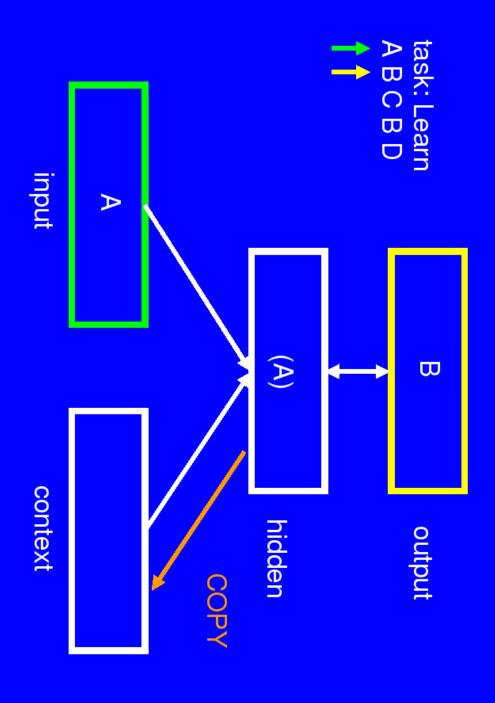


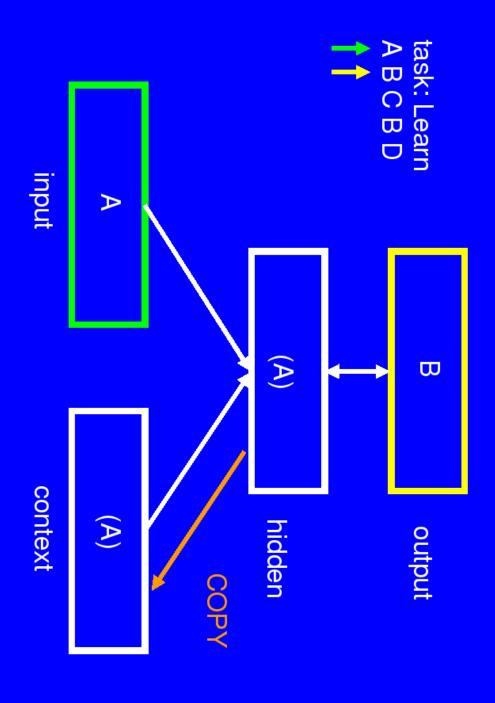


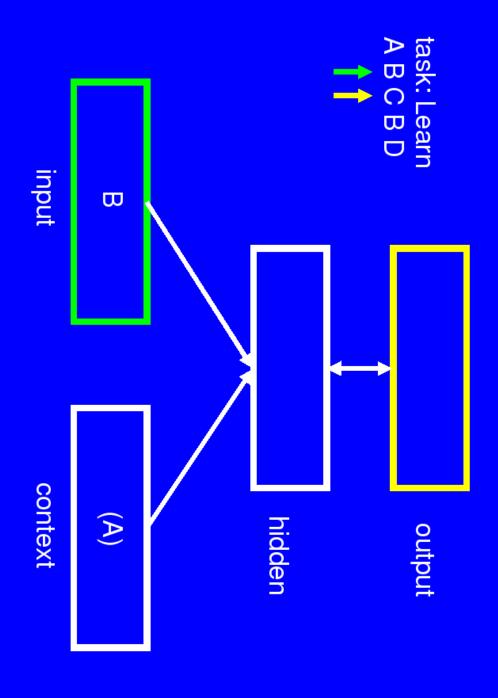


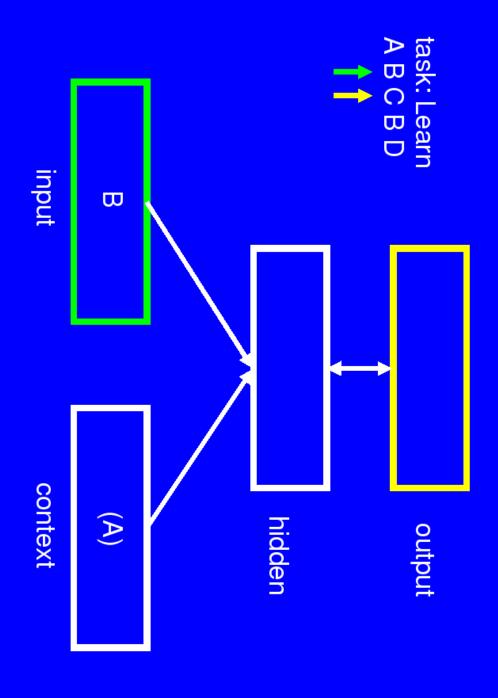


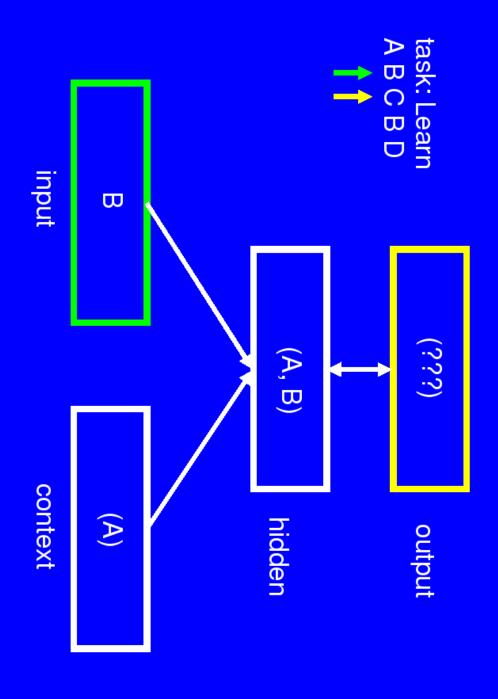


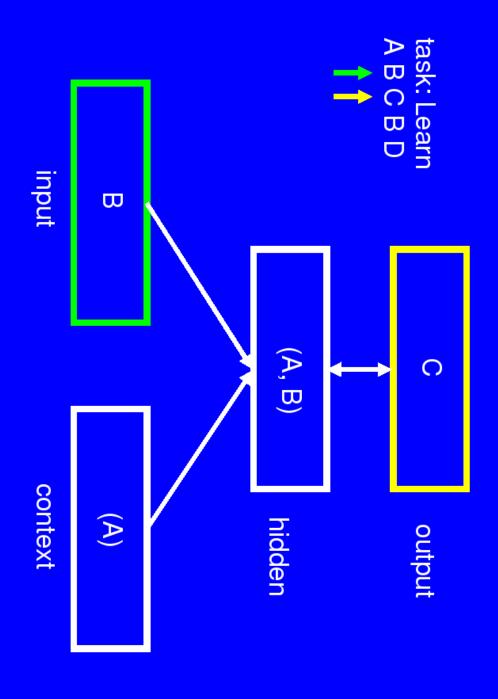


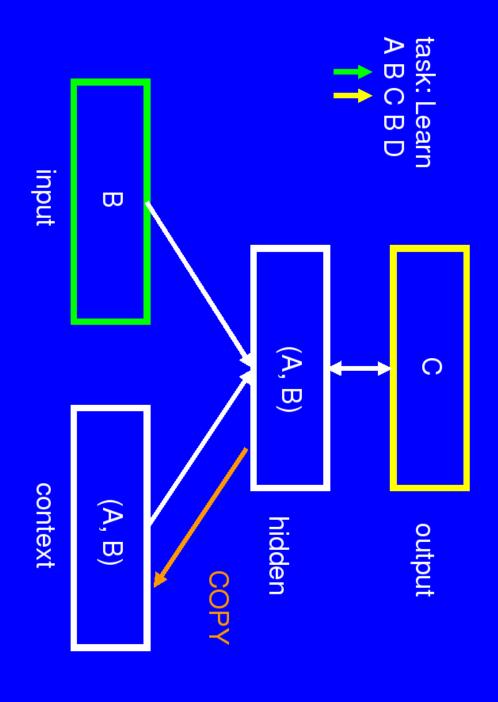


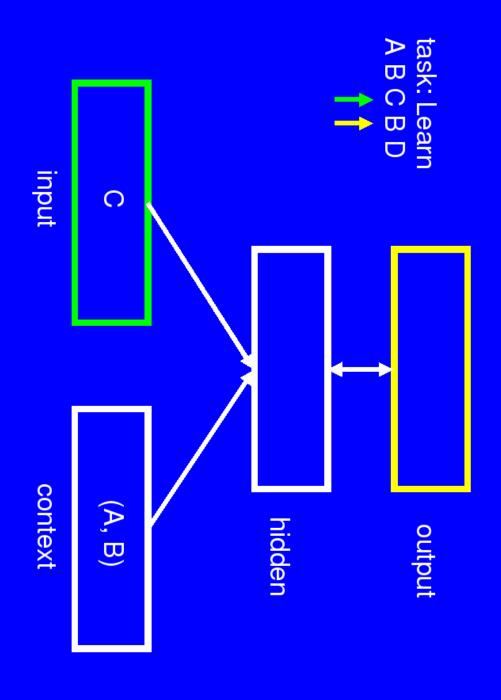


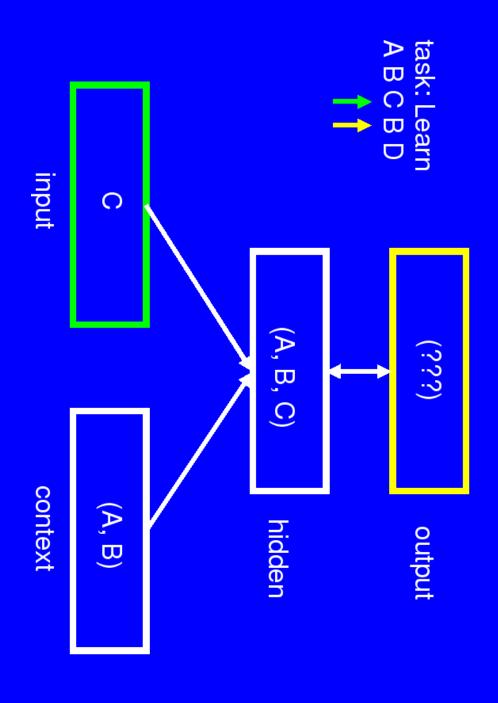


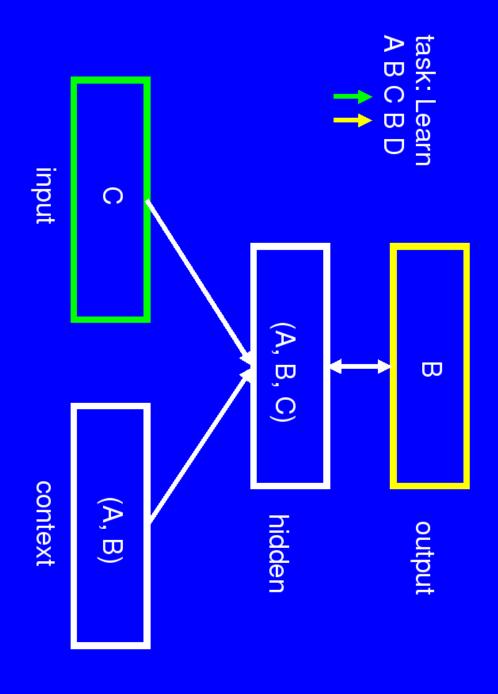


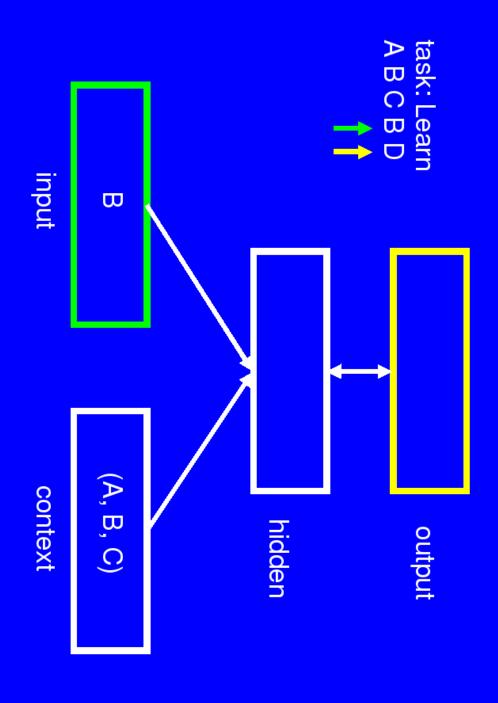






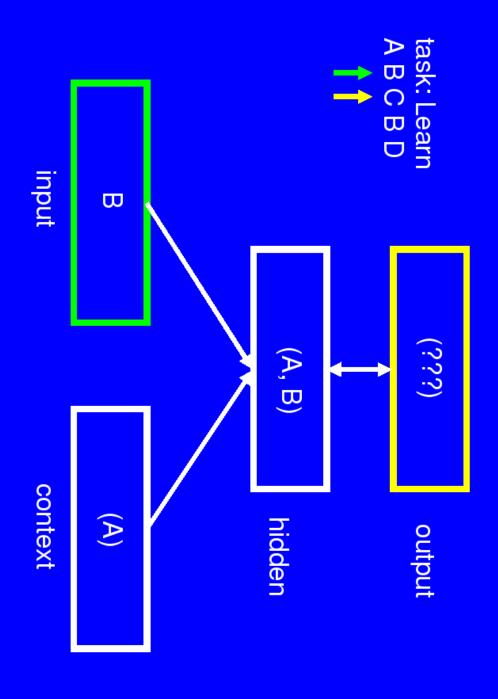


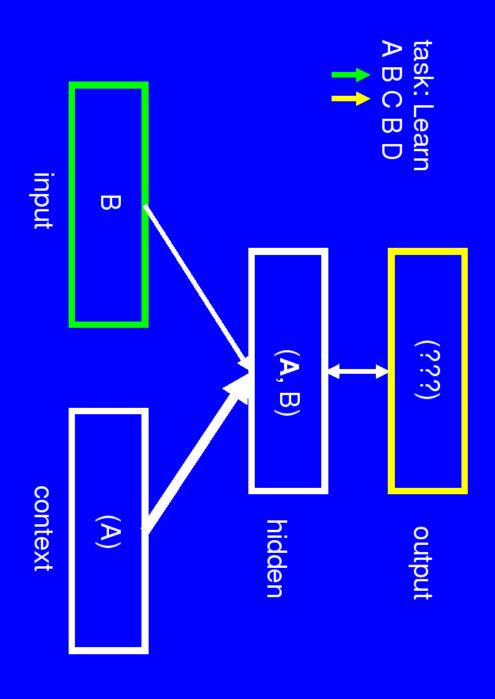


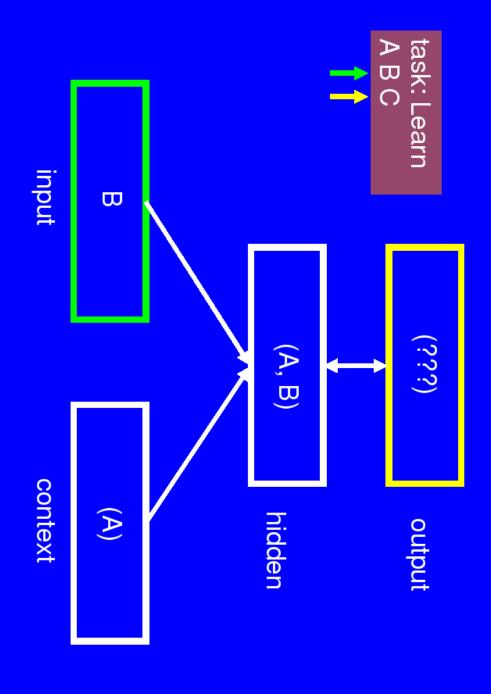


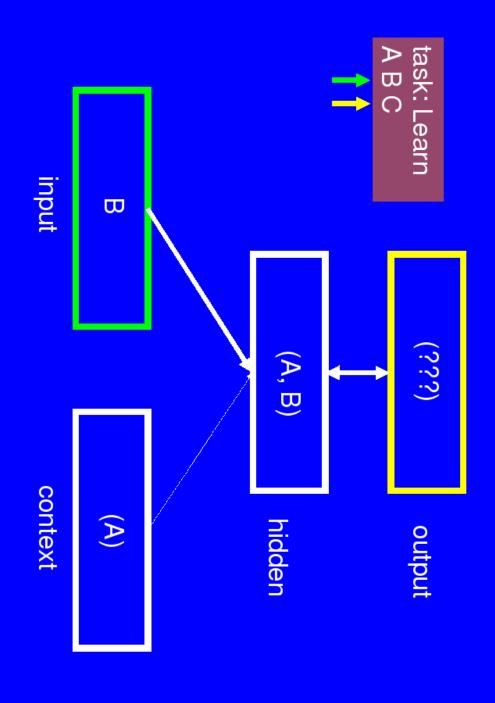
Why Copy the Hidden Representation?

- Copying input or output only lets the network hold on to one previous
- Copying the hidden layer lets the network hold on to an arbitrarily large number of items – even though it is always just copying last hidden state at time t-1.
- The network learns how strongly to hold on to past items

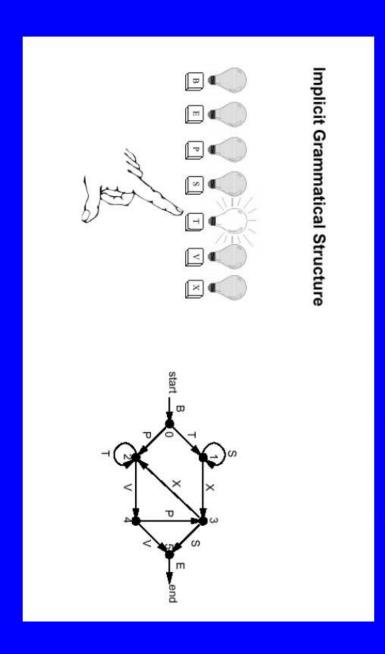








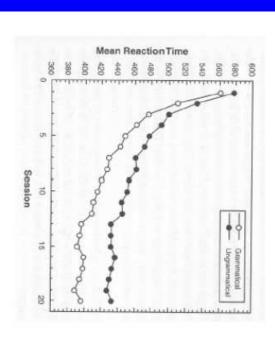
Artificial Grammar Learning



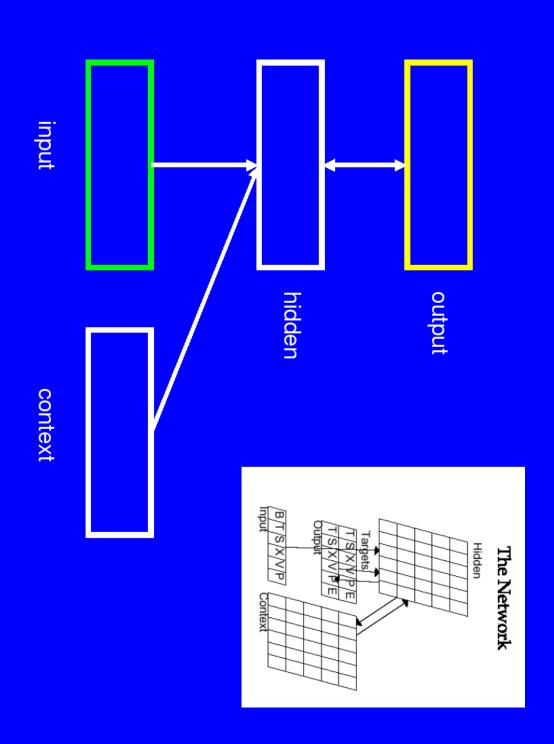
Task: Press buttons that implicitly follow the grammar

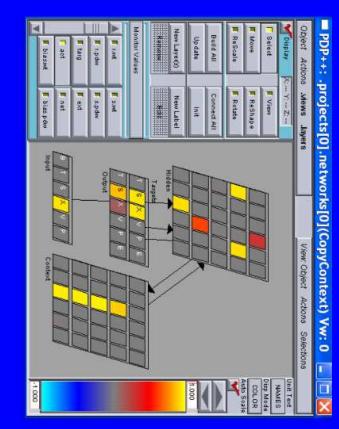
Note: Subjects do not know about the grammar!

Evidence For Implicit Learning



- Response times are lower for grammatical sequences.
- Learners report no knowledge of a sequential pattern.
- Learners are at chance when asked to predict the next light.



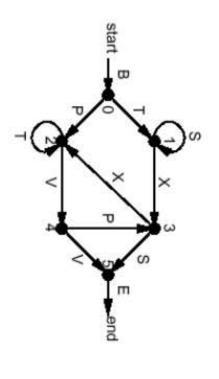


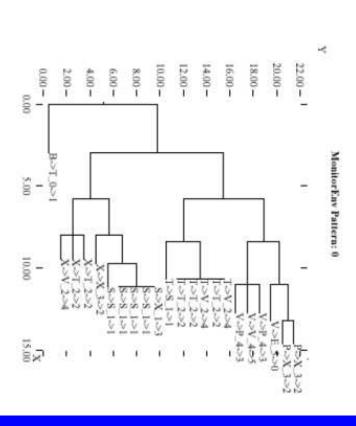
Some details:

- Input patterns: Generated (randomly) using the finite state grammar
- Sometimes there are multiple "correct" answers for what answer comes next. kWTA forces the network to guess one

Hidden Activity Reflects State Information

input, is available in the pattern of hidden layer activity. Grammatical state information, along with information concerning the last





Simple SRN story is not flawless

- How is hidden→ "copy" function implemented biologically?
- During settling, context must be actively maintained (ongoing hidden activity has no effect on context).
- context. Assumes all context is relevant: What if distracting information presented in middle of sequence? Want to only hold on to *relevant*
- updating / gating vs. robust maintenance of context. → Stay tuned for specialized biological/computational mechanisms for

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e.g., Why am I here today, instead of lying on a beach in Mexico, drinking mojitos and reading a good book?

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mojitos and reading a good book? e.g., Why am I here today, instead of lying on a beach in Mexico, drinking

Challenge: make a responsible neural network!

The Motivational Bootstrap

- Some motivations must be built-in (else we would die)
- Where do art/science come from?
- Need to learn on top of built-in drives

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Culture & social drives provide cumulative shaping of learning.

So, why does anyone go to university?

- Socially-mediated standards of success.
- Strong built-in desire to share w/others.
- Strong built-in desire to learn (dopamine?)

What I'm Actually Talking About

Skinnerian learning

The basic stuff that every mammal has in common:

(from a computational perspective). Neural mechanisms of Pavlovian conditioning

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No supervised target signal available: only good/bad outcomes Enables bootstrap of new stimuli (CS's) onto built-in desires (US's):

 $CS (money) \rightarrow US (food, etc)$

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Skinnerian learning

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(from a computational perspective). Neural mechanisms of Pavlovian conditioning

Enables bootstrap of new stimuli (CS's) onto built-in desires (US's): No supervised target signal available: only good/bad outcomes

 $CS (money) \rightarrow US (food, etc)$

But what if consequence of given input comes later in time?

Temporally-Extended Tasks with Sparse Rewards





Temporally-delayed Learning & Reinforcement

need to "span the gap". Reinforcement often delayed from the events that lead to it:

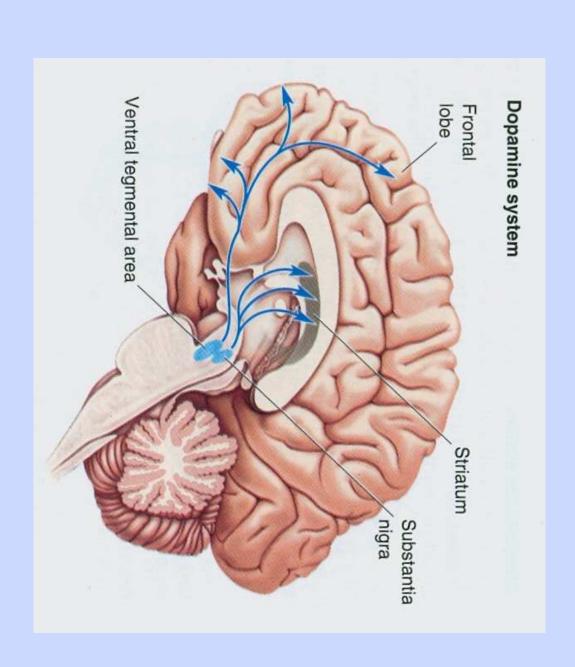
Temporally-delayed Learning & Reinforcement

need to "span the gap". Reinforcement often delayed from the events that lead to it:

Key idea:

- We want to predict future rewards consistently over time.
- This allow us to learn what events are associated with rewards, earlier and earlier back in time.

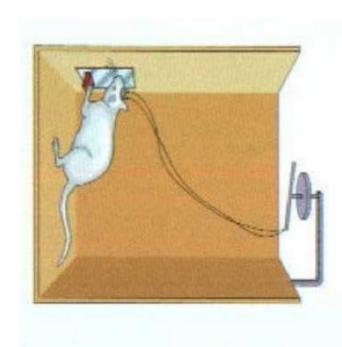
We use the Temporal Differences (TD) algorithm (Sutton & Barto).





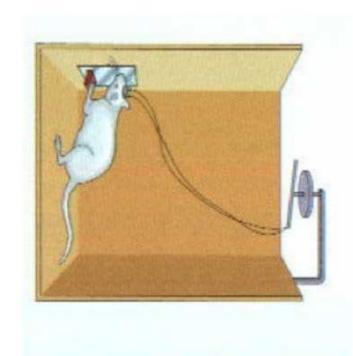


Dopamine carries the brain's reward signal



Wise & Romper, 89

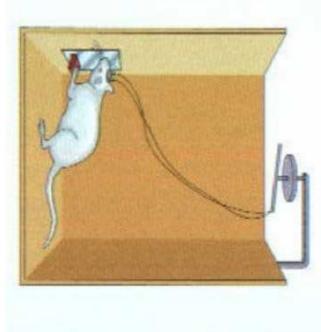
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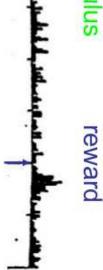
stimulus reward

Wise & Romper, 89

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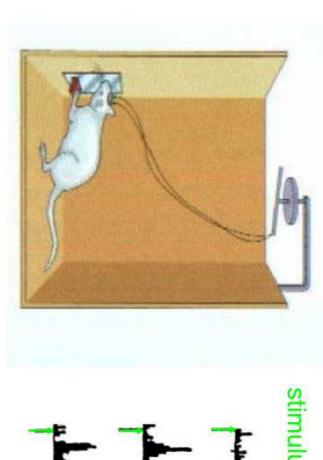
stimulus



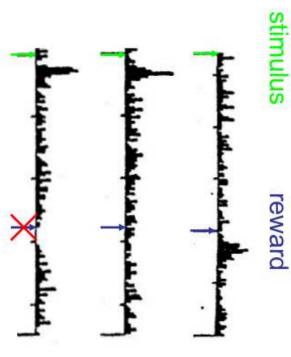
Schultz et. al, 98

Wise & Romper, 89

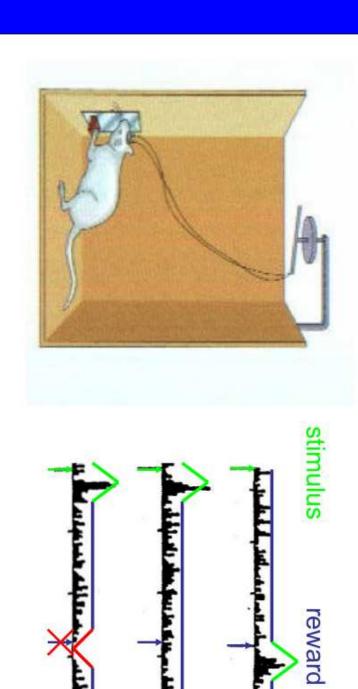
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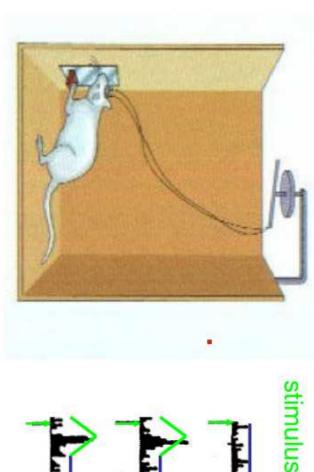


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Wise & Romper, 89

Dopamine carries the brain's revard signal reward prediction error

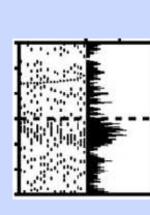


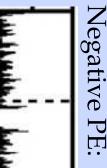
Wise & Romper, 89

Reinforcement learning and dopamine: prediction errors

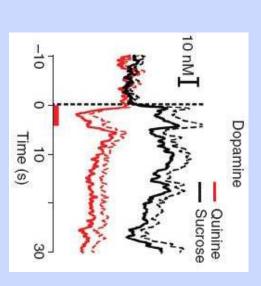
Positive PE:



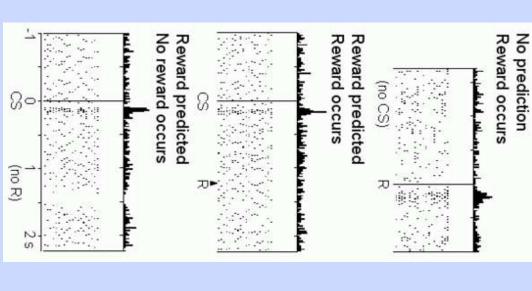






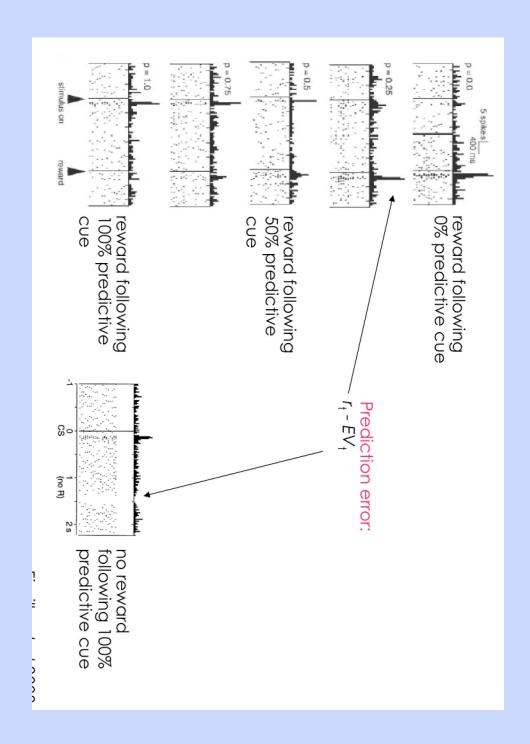


Basic Data: VTA dopamine firing in Conditioning

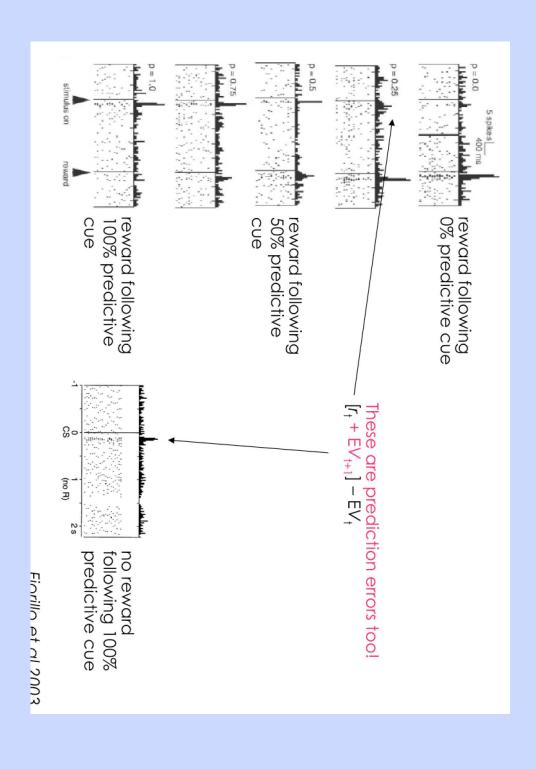


Schultz, Montague & Dayan, 2007

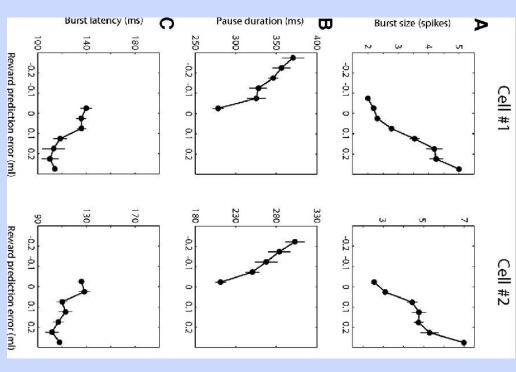
Dopamine and Reward Probability



Dopamine and Reward Probability



Burst/Pause correlations with Rew Prediction Errors



Bayer et al, 2007 JNeurophys

Value function, sum of discounted future rewards:

$$V(t) = \langle \gamma^0 r(t) + \gamma^1 r(t+1) + \gamma^2 r(t+2) \dots \rangle$$
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Error in predicted reward (from previous to next time-step):

$$\delta(t) = \left(r(t) + \gamma \hat{V}(t+1)\right) - \hat{V}(t) \tag{3}$$

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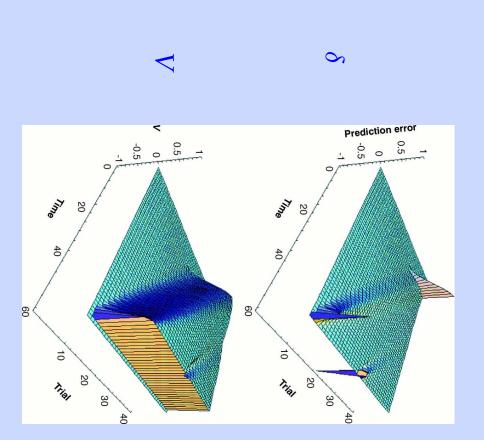
Update value estimate:

$$\widehat{V}(t) \leftarrow \widehat{V}(t) + \alpha \delta(t) \tag{4}$$

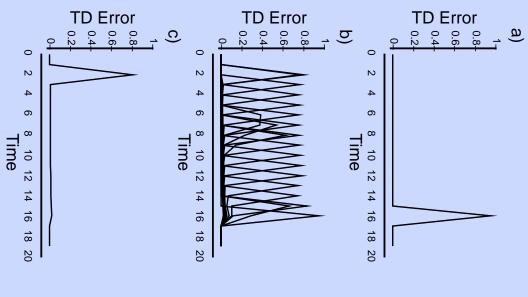
 α = learning rate

TD and Dopamine Relationship

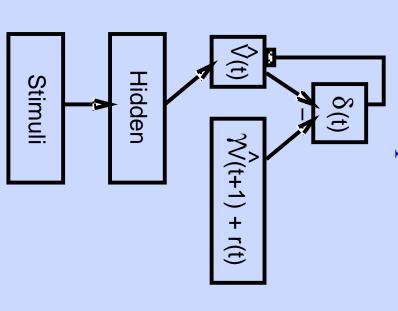
Schultz, Dayan & Montague, 1997, Science



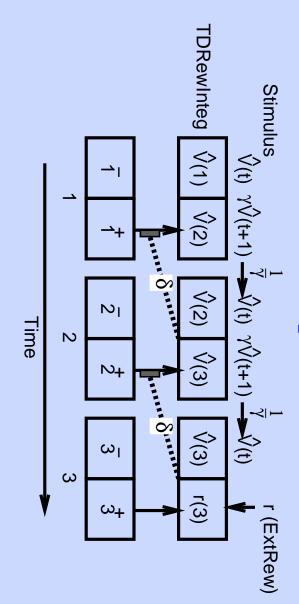
Model: CS at t=2, US at t=16



Network Implementation



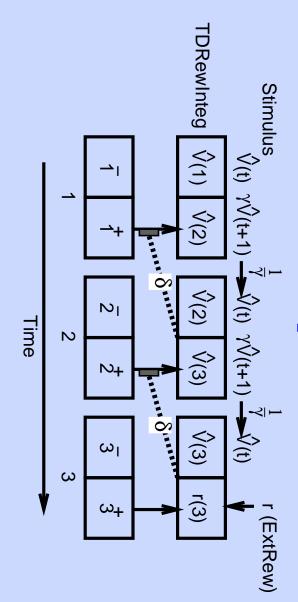
Phase-based Implementation



TDRewInteg = TDRewPred + ExtRew

Minus phase: TDRewInteg clamped to prev plus phase value.

Phase-based Implementation



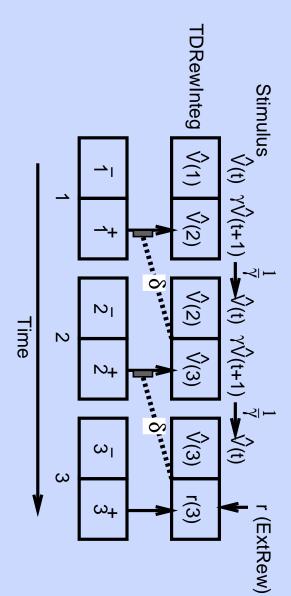
TDRewInteg = TDRewPred + ExtRew

Minus phase: TDRewInteg clamped to prev plus phase value.

Plus phase: TDRewInteg settles via weights

= expected reward at t+1, plus any ExtRew at time t.

Phase-based Implementation

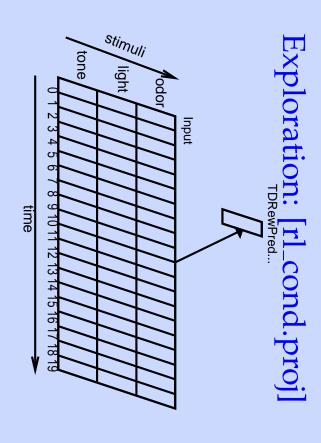


TDRewInteg = TDRewPred + ExtRew

Minus phase: TDRewInteg clamped to prev plus phase value.

Plus phase: TDRewInteg settles via weights = expected reward at t+1, plus any ExtRew at time t.

(eligibility traces needed) Learning signal δ (= "TD") trains prediction for *previous* time step.



(used in Sutton & Barto, Montague et al, etc) unique unit for each stimulus at each time point 'Complete Serial Compound' (CSC) input representation:

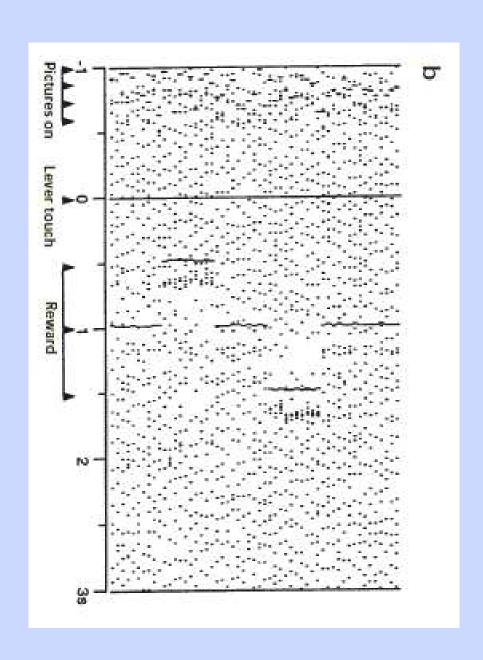
Not realistic, but good for demonstration. This assumption can be relaxed without changing core ideas (e.g. Ludvig et al, 2008).

Exploration: [rl_cond.proj]

Standard TD: $\hat{V}(t) = \sum_i w_i x_i(t)$ [x_i are inputs: tone, light]

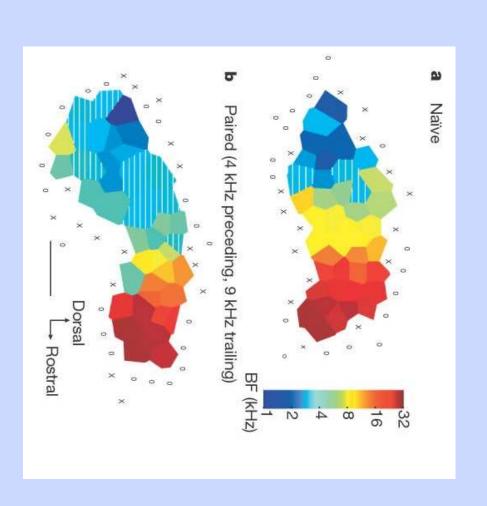
inhibitory competition from other value reps Here: passed thru activation function – has to surpass threshold, subject to

DA and Timing: Late and Early Rewards

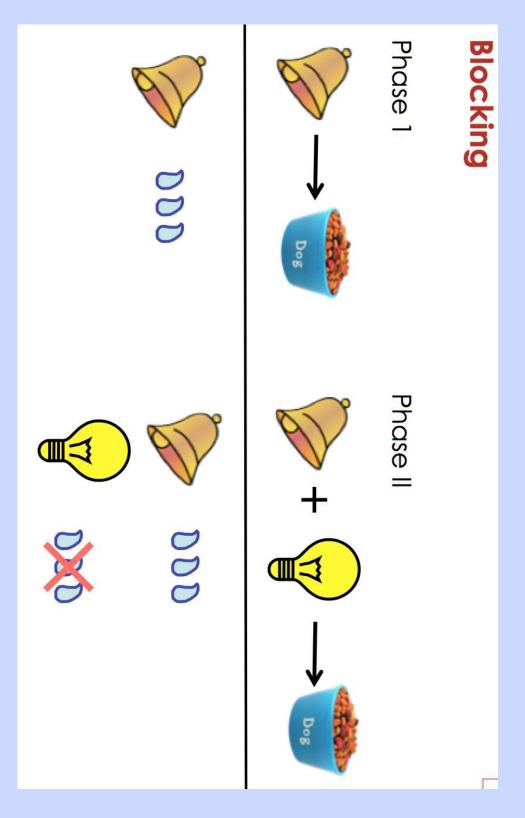


DA and Learning: Auditory Cortex

Bao et al, 2001, Nature

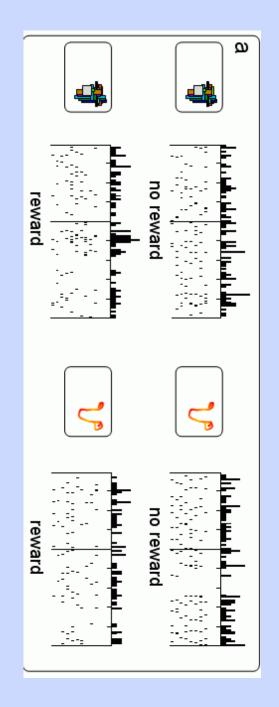


Learning Theory: Blocking (Behavior)



Learning Theory: Blocking (Dopamine)

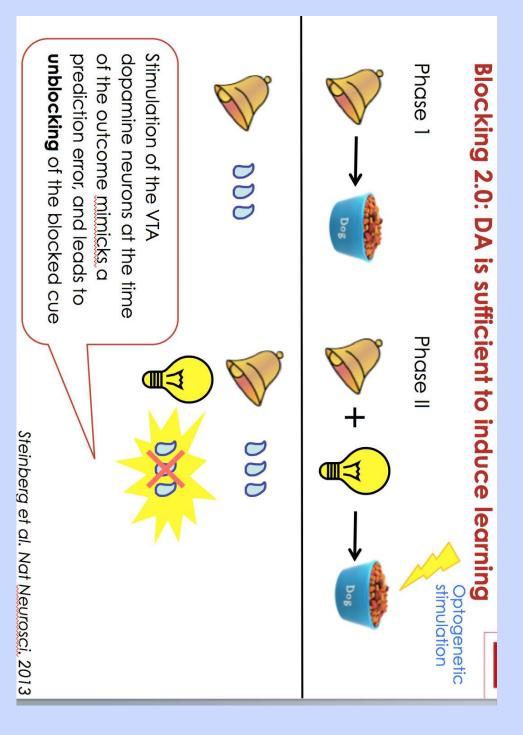
Waelti et al, 2001, Nature



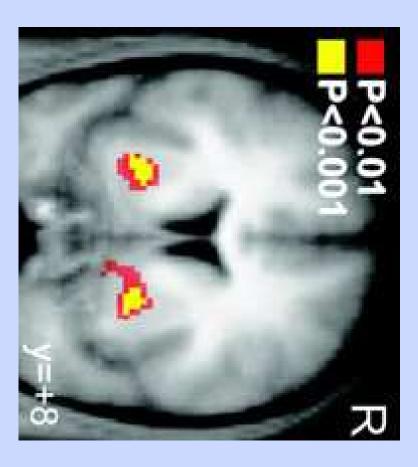
Blocked stimulus

Control (not blocked) stim

Learning Theory: (Un)Blocking

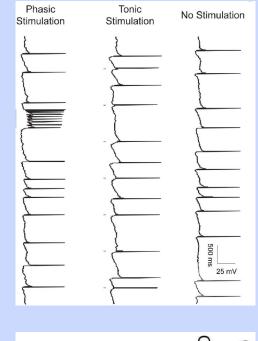


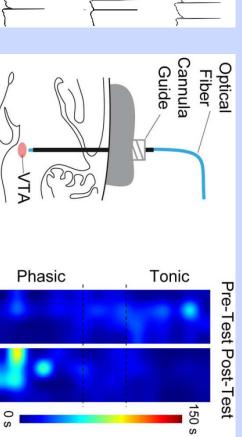
O'Doherty et al, 2004, Science TD prediction error and human functional imaging



Ventral striatum = DA enriched, correlates with TD PE=Critic!

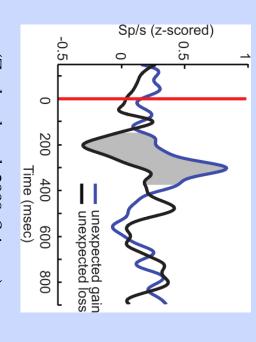
ptical phasic DA stimulation causally induces conditioning





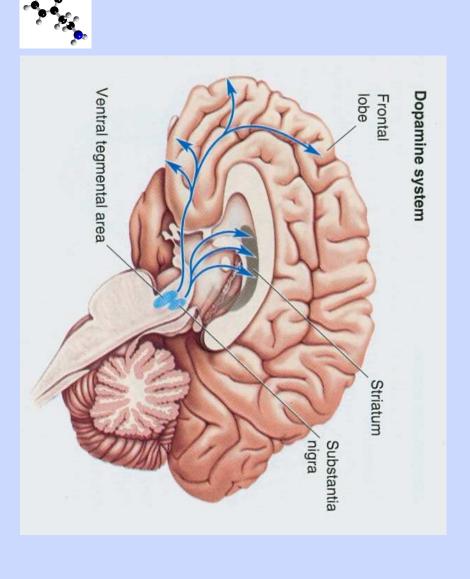
(Tsai et al, 2009, Science)

DA neuron spiking during reinforcement task in humans



(Zaghoul et al, 2009, Science)

How are dopamine-based RPE signals used to select actions?



Will consider biological implementation in basal ganglia later

Q learning: extending prediction error learning to actions

Error in predicted reward:

$$\delta_t = \left(r_t + \gamma \max_a Q_t(s_{t+1}, a)\right) - Q_t(s, a)$$

Update value estimate:

$$Q_t(s,a) \leftarrow Q_t(s,a) + \alpha \delta(t)$$

Select among Q values:

$$P_t(a) = \frac{e^{\frac{Q_t(s,a)}{\beta}}}{\sum_{i=1}^n e^{\frac{Q_t(s,i)}{\beta}}}$$

 γ = discount, α = learning rate, β = "temperature" / exploration parameter

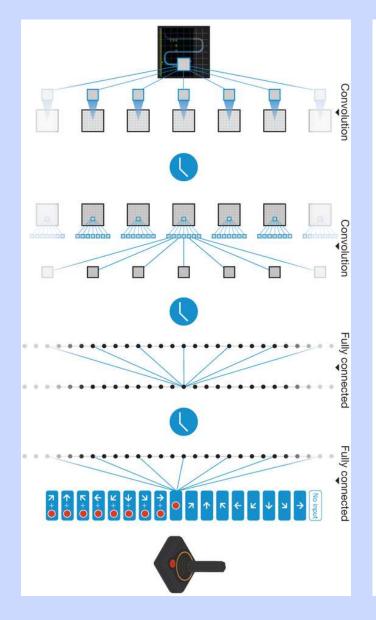
Google Deep Mind RL Network ("DQN") Plays Atari

ETTER

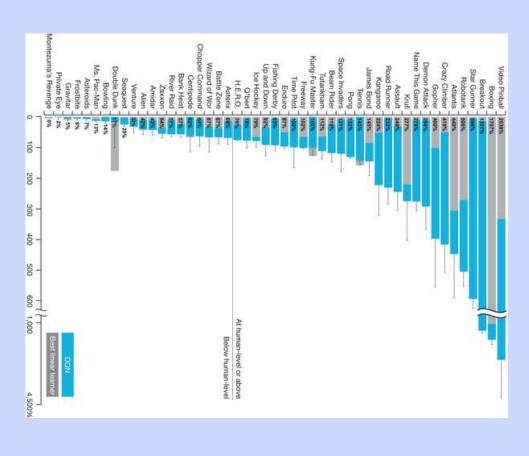
doi:10.1038/nature14236

Human-level control through deep reinforcement learning

Volodymyr Mnih^{1*}, Koray Kavukcuoglu^{1*}, David Silver^{1*}, Andrei A. Rusu¹, Joel Veness¹, Marc G. Bellemare¹, Alex Graves¹, Martin Riedmiller¹, Andreas K. Fidjeland¹, Georg Ostrovski¹, Stig Petersen¹, Charles Beattie¹, Amir Sadik¹, Ioannis Antonoglou¹, Helen King¹, Dharshan Kumaran¹, Daan Wierstra¹, Shane Legg¹ & Demis Hassabis¹



Google Deep Mind RL Network ("DQN") Plays Atari



Extra

powerful. This material is optional for the course. PVLV, which we think is more biologically plausible and computationally The following slides describe a recently developed alternative to TD, called

The Problem

stimuli? Q: How do we learn to attach positive/negative valence to environmental

The Problem

stimuli? Q: How do we learn to attach positive/negative valence to environmental

A: The same way we learn lots of other stuff: the Delta Rule!

$$\delta_{pv} = r - \hat{V}_{pv}$$

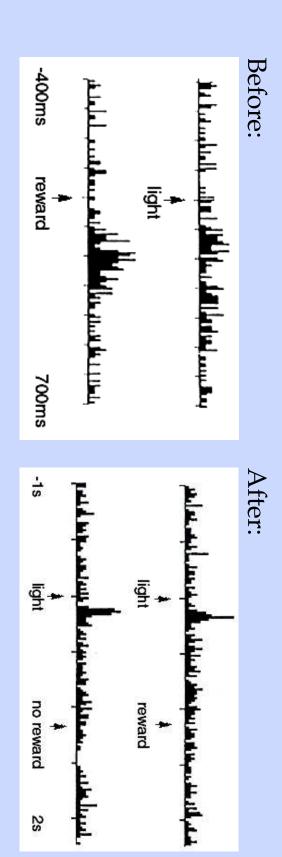
 \hat{V}_{pv} : expected reward based on prior associations

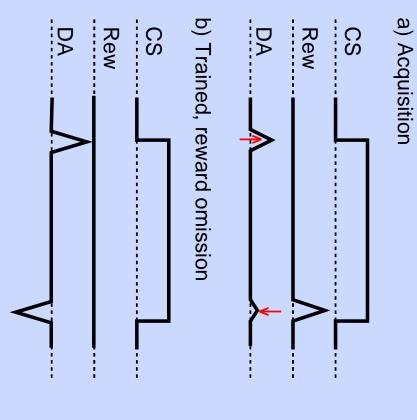
r: reward

 δ_{pv} : learning signal

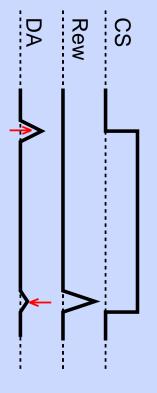
The Problem

Q: But what happens when environmental stimulus occurs before reward?

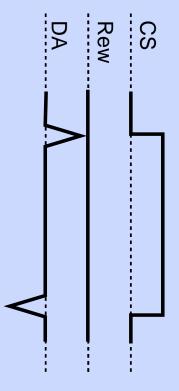






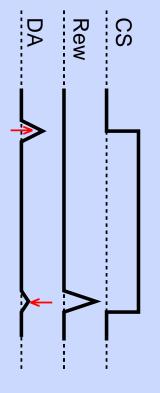


b) Trained, reward omission

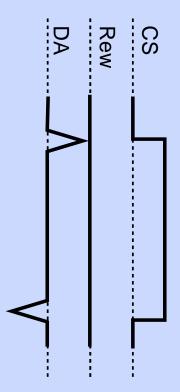


Dopamine spikes/dips are learning signals





b) Trained, reward omission



Dopamine spikes/dips are learning signals

Delta rule fails to account for predictive DA spike!

Standard Approach: TD

Predict all future rewards (discounted):

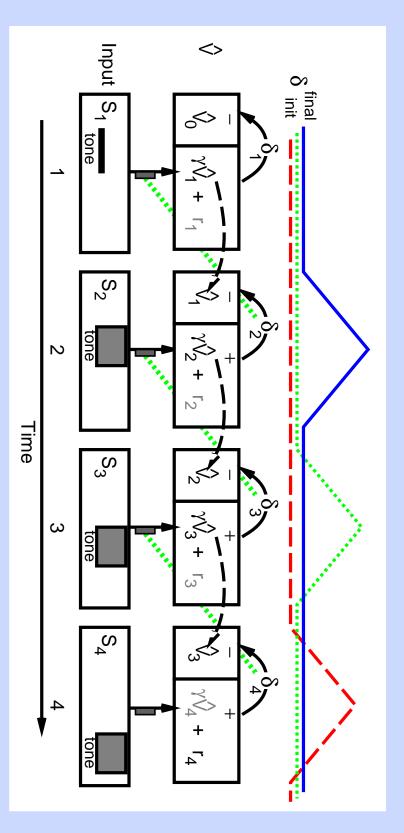
$$V_t = \sum_{\tau=t+1}^{\tau=\infty} \gamma^{\tau-(t+1)} r_{\tau}$$

Recursively:
$$\hat{V}_{t-1} = r_t + \gamma \hat{V}_t$$

Error = Temporal Difference = TD:

$$DA = \delta_t = [r_t + \gamma \hat{V}_t] - \hat{V}_{t-1}$$

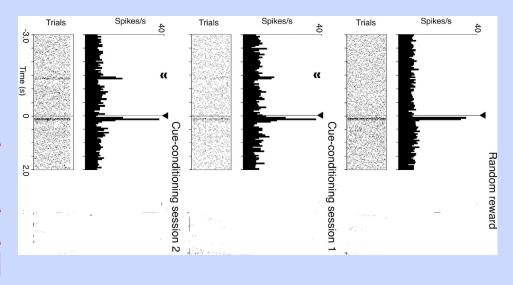
TD Illustrated



Problems with TD

- Great algorithm, developed in computer science / machine learning, but is this actually what the brain does?
- Even if so, doesn't specify how these signals are computed by systems upstream of DA... just predicts DA and δ but says nothing about V, etc.
- Current reward value is always relative to what happened just before. Too much temporal dependency?
- Chaining not seen in neural recordings.
- What determines "discount factor" γ , biologically?

Pan et al, 2005, Journal of Neuroscience CS and US DA spike

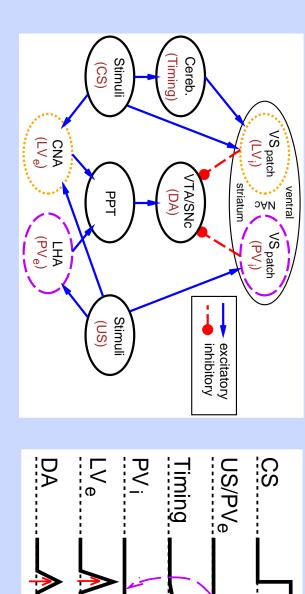


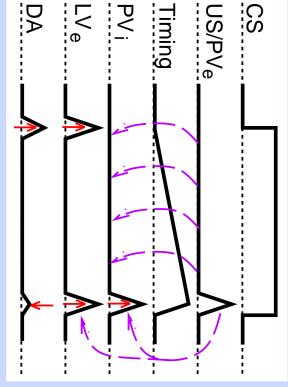
Inconsistent with standard TD!

The PVLV Alternative

(O'Reilly, Frank, Hazy & Watz, 2007, Behav Neurosci) PVLV = Primary Value, Learned Value

- No reward predictions, just associations!
- No temporal dependencies: DA depends only on current state.
- Uses same basic delta-rule learning as TD (Rescorla-Wagner).





- PV (Primary Value): Primary rewards (US), canceled.
- LV (Learned Value): Learned associations (CS \rightarrow DA).

PV: Primary Value

Trained at each point in time on actual reward value present:

$$\delta_t = r_t - \widehat{V}_t$$

PV: Primary Value

Trained at each point in time on actual reward value present:

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This uses immediate prediction (\hat{V}_t) of current rew value (r_t)

PV: Primary Value

Trained at each point in time on actual reward value present:

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- This uses immediate prediction (\hat{V}_t) of current rew value (r_t)
- Accounts for canceling of DA spike @ rew, and DA dips when no rew received.

PV: Primary Value

Trained at each point in time on actual reward value present:

$$\delta_t = r_t - V_t$$

- This uses immediate prediction (\tilde{V}_t) of current rew value (r_t)
- Accounts for canceling of DA spike @ rew, and DA dips when no rew received.
- But this doesn't account for predictive DA spikes... (actually results in predictive DA dips!)

LV: Learned value

Represents perceived values of stims even when there is no current rew expectation.

LV: Learned value

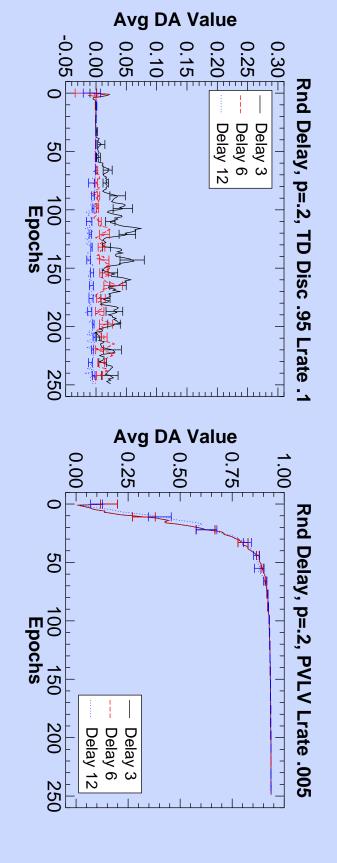
- Represents perceived values of stims even when there is no current rew expectation.
- Only gets training signal @ rew, or when PV expects some rew. (ie learning is filtered by primary PV system.)

LV: Learned value

- Represents perceived values of stims even when there is no current rew expectation.
- Only gets training signal @ rew, or when PV expects some rew. (ie learning is filtered by primary PV system.)
- → Learns at time of rew, but not at CS onset.
- \rightarrow Generalizes rew values to CS...
- associated with reward! → Accounts for DA spikes for stimuli that have previously been

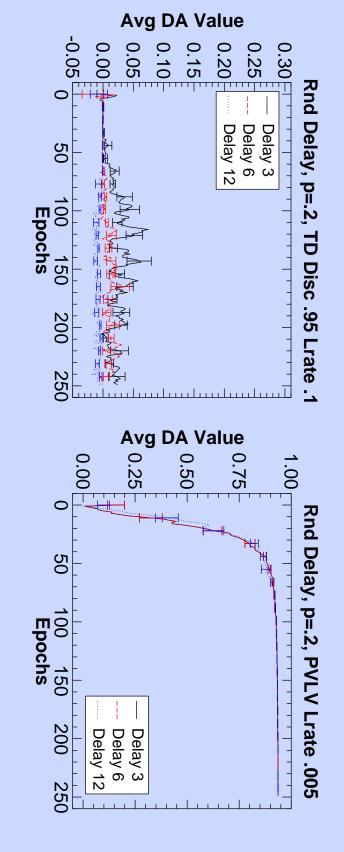
PVLV: Computationally Powerful

Comparison with TD on Random Delays (breaks TD chaining):



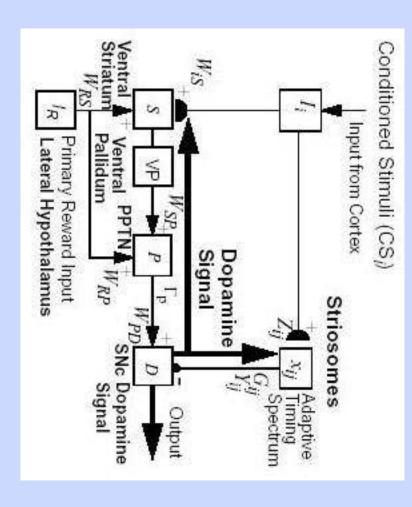
PVLV: Computationally Powerful

Comparison with TD on Random Delays (breaks TD chaining):



Enables working memory model to learn complex WM tasks.

Similar to Brown, Bullock & Grossberg, '99



Functional (intrinsic timing? LV system cannot train itself). Diffs: Anatomical (CNA vs. VS; Dorsal vs. Ventral Patch)

PVLV accounts for timing data better than TD!

- activation. Data: during transient learning period, both rews and CS elicit
- This accounted for by PV, LV systems operating in parallel.
- TD: predicts chaining back in time from rew to CS.

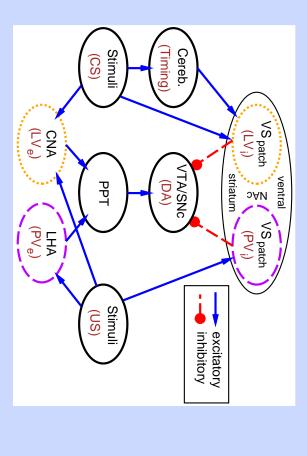
PVLV accounts for timing data better than TD!

- Data: delayed rewards cause dips @ usual time, then spikes
- This accounted for by both TD and PV.

PVLV accounts for timing data better than TD!

- Data: delayed rewards cause dips @ usual time, then spikes
- This accounted for by both TD and PV.
- Data: early rewards cause spikes, then dips @ usual time
- spike. This accounted for by PV (spike), PV (dip), but TD only accounts for

More Key Predictions from PVLV



- CNA = Pavlovian conditioning (e.g., Killcross et al. '97).
- NAc (patch/shell) = Extinction (Ferry et al. '00; Annett et al., 89), Blocking (data?).
- NAc (matrix/core) = Basic actions (OR's, approach, avoid)
- CNA can't train itself: No 2nd order conditioning!
- BLA = 2nd order cond, uses
 DA-independent mechanisms
 (CNA/BLA double-dissoc).

Conclusions

that seems to fit with biology & behavioral data. PVLV provides computationally motivated architecture

into our fixed set of built-in motivational drives. These learning mechanisms enable arbitrary stimuli/goals to be plugged

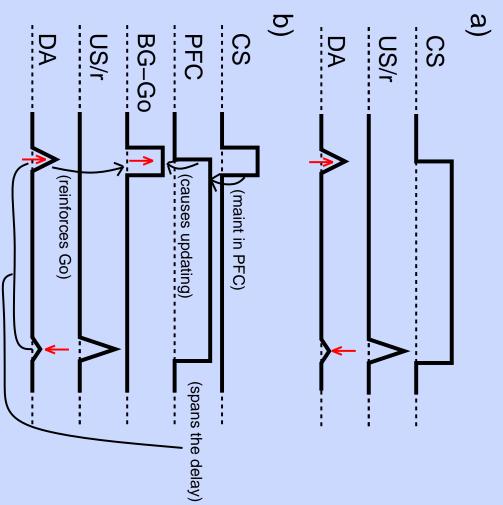
Conclusions

that seems to fit with biology & behavioral data. PVLV provides computationally motivated architecture

into our fixed set of built-in motivational drives. These learning mechanisms enable arbitrary stimuli/goals to be plugged

Something motivates every generated mental-state, always!

PVLV, WM, and DA



PVLV: Two Separate Mechanisms (PV, LV)

PV learning:

$$\delta_{pv} = r - \hat{V}_{pv}$$

 $\Delta w_i = \epsilon x_i \delta_{pv}$

$$\delta_{pv} = PV_e - PV_i$$

PVLV: Two Separate Mechanisms (PV, LV)

PV learning:

$$\delta_{pv} = r - \widehat{V}_{pv}$$

$$\delta_{pv} = PV_e - PV_i$$

$$\Delta w_i = \epsilon x_i \delta_{pv}$$

LV learning (filtered by PV):

$$\Delta w_i = \begin{cases} \epsilon (r_t - \hat{V}_{lv}) x_i & \text{if } \hat{V}_{pv} > \theta_{pv} \text{ or } r_t > 0 \\ 0 & \text{otherwise} \end{cases}$$

PVLV: Two Separate Mechanisms (PV, LV)

PV learning:

$$\delta_{pv} = r - \hat{V}_{pv}$$
 -or- $\delta_{pv} = PV_e - PV_i$

$$\Delta w_i = \epsilon x_i \delta_{pv}$$

LV learning (filtered by PV):

$$\Delta w_i = \begin{cases} \epsilon (r_t - \hat{V}_{lv}) x_i & \text{if } \hat{V}_{pv} > \theta_{pv} \text{ or } r_t > 0 \\ 0 & \text{otherwise} \end{cases}$$

Global DA (PV dominates):

$$\delta_t = \begin{cases} \delta_{pv} & \text{if } \widehat{V}_{pv} > \theta_{pv} \text{ or } r_t > 0 \\ \delta_{lv} & \text{otherwise} \end{cases}$$

$$\delta_{lv} = LV_e - LV_i$$

LV Extras

DA spikes only observed @ CS onset, don't continue throughout delay until reward. Problem for PV?

LV Extras

- DA spikes only observed @ CS onset, don't continue throughout delay until reward. Problem for PV?
- Solution: PV system has synaptic depression, accommodates to constant sensory inputs; only perceives values of stims that were not present in last time step.
- This is also important for PFC learning.. (stay tuned)